

**BENHA UNIVERSITY  
FACULTY OF ENGINEERING (SHOUBRA)  
ELECTRONICS AND COMMUNICATIONS ENGINEERING**



# ECE 444

# Industrial Electronics

(2022 - 2023) 1<sup>st</sup> term

Lecture 3: Definitions.

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# Outlines:

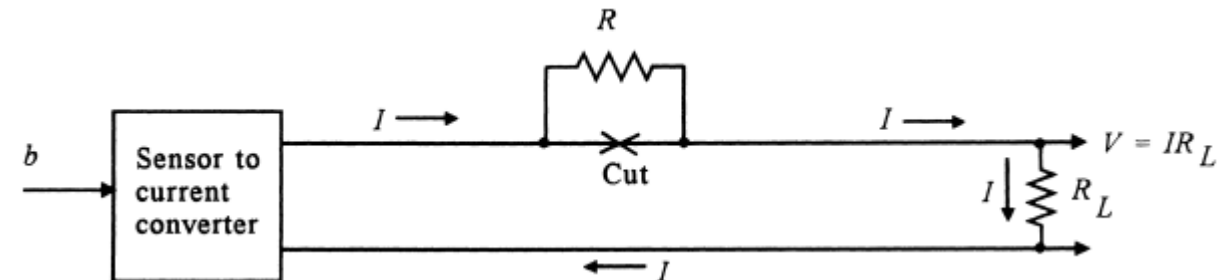
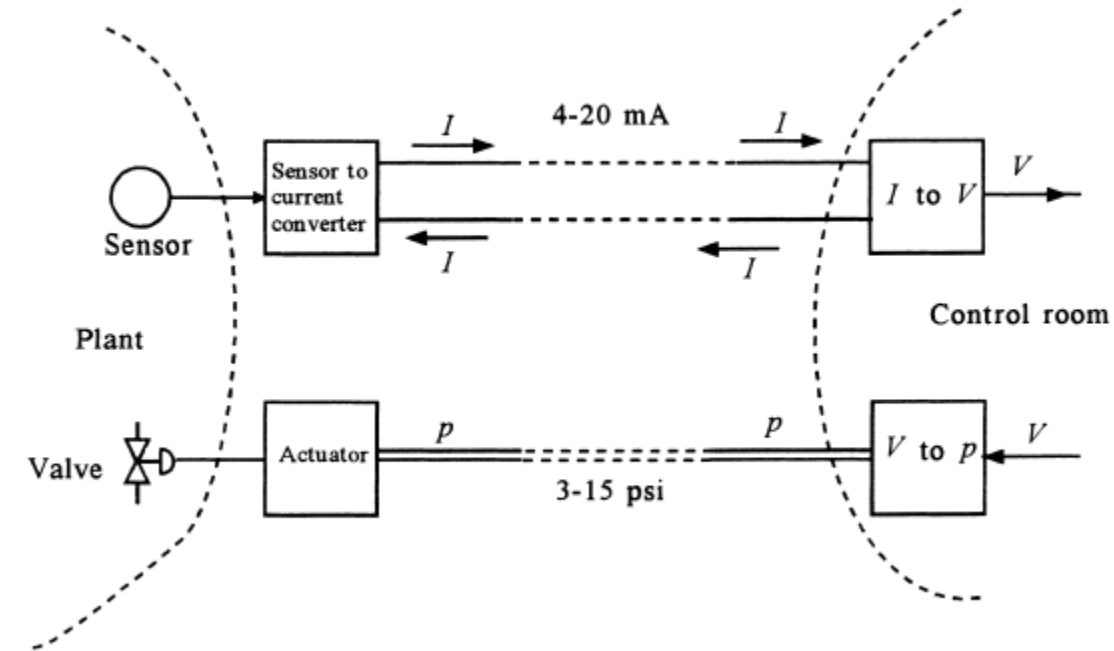
- Analog Data Representation.
- Error.
- Transfer Function.
- Accuracy.
- System Accuracy.
- Sensitivity.
- Hysteresis.

# Analog Data Representation:

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- For measurement systems or control systems, part of the specification is **the range of the variables involved**.
- Two analog standards are in common use as a means of representing the range of variables in control systems.
  - 1) For **electrical** systems, we use a range of **electric current** carried in wires.
  - 2) For **pneumatic** systems we use a range of **gas pressure** carried in pipes.

❖ Why current not voltage !?



# Analog Data Representation:

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**EXAMPLE 7** Suppose the temperature range  $20^{\circ}$  to  $120^{\circ}\text{C}$  is linearly converted to the standard current range of 4 to 20 mA. What current will result from  $66^{\circ}\text{C}$ ? What temperature does 6.5 mA represent?

*Solution*

The easiest way to solve this kind of problem is to develop a linear equation between temperature and current. We can write this equation as  $I = mT + I_0$ , and we know from the given data that  $I = 4$  mA when  $T = 20^{\circ}\text{C}$  and that  $I = 20$  mA when  $T = 120^{\circ}\text{C}$ . Thus, we have two equations in two unknowns:

$$4 \text{ mA} = (20^{\circ}\text{C})m + I_0$$

$$20 \text{ mA} = (120^{\circ}\text{C})m + I_0$$

$$\text{so that } m = 0.16 \text{ mA}/^{\circ}\text{C} \qquad I_0 = 0.8 \text{ mA}$$

Thus, the equation relating current and temperature is

$$I = (0.16 \text{ mA}/^{\circ}\text{C})T + 0.8 \text{ mA}$$

Now answering the questions is easy. For  $66^{\circ}\text{C}$ , we have

$$I = (0.16 \text{ mA}/^{\circ}\text{C})66^{\circ}\text{C} + 0.8 \text{ mA} = \mathbf{11.36 \text{ mA}}$$

For 6.5 mA, we solve for  $T$ :

$$6.5 \text{ mA} = (0.16 \text{ mA}/^{\circ}\text{C})T + 0.8 \text{ mA}$$

for which  $T = \mathbf{35.6^{\circ}\text{C}}$ .

➤ In **measurement**:

Error = Actual value – Measured indication of the value

Is actual value be known? .....No

So use **accuracy** to place bounds on the **possible error**.

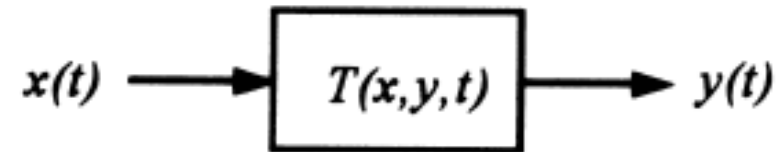
➤ In **control system**:

Error of the controlled variable = **Desired value - Measured value**

# Transfer Function:

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- A transfer function shows how a system-block output variable varies in response to an input variable, as a function of both static input value and time.



- The transfer function is often described in two parts:
  - 1) **Static** Part (when the input is not changing in time)
    - ➔ represented by **Equations – Tables – Graphs**
  - 2) **Dynamic** Part (when there is time variation of the input)
    - ➔ represented by **Differential Equations**
- T.F. is **valid** only over **a certain range of variable values**.

# Accuracy:

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➤ It is the max. expected overall error from a device.

➤ Forms:

1) Measured variable  $\pm 2\sigma$

2) % of full-scale  $\pm 0.5\%$  FS

3) % of span  $\pm 0.5\%$  Span

4) % of the actual reading  $\pm 1\%$  of reading

**EXAMPLE 8** A temperature sensor has a span of  $20^{\circ}\text{--}250^{\circ}\text{C}$ . A measurement results in a value of  $55^{\circ}\text{C}$  for the temperature. Specify the error if the accuracy is **(a)**  $\pm 0.5\%$  FS, **(b)**  $\pm 0.75\%$  of span, and **(c)**  $\pm 0.8\%$  of reading. What is the possible temperature in each case?

### *Solution*

Using the given definitions, we find

- a.** Error =  $(\pm 0.005)(250^{\circ}\text{C}) = \pm 1.25^{\circ}\text{C}$ . Thus, the actual temperature is in the range of  $53.75^{\circ}$  to  $56.25^{\circ}\text{C}$ .
  - b.** Error =  $(\pm 0.0075)(250 - 20)^{\circ}\text{C} = \pm 1.725^{\circ}\text{C}$ . Thus, the actual temperature is in the range of  $53.275^{\circ}$  to  $56.725^{\circ}\text{C}$ .
  - c.** Error =  $(\pm 0.008)(55^{\circ}\text{C}) = \pm 0.44^{\circ}\text{C}$ . Thus, the temperature is in the range of  $54.56^{\circ}$  to  $55.44^{\circ}\text{C}$ .
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**EXAMPLE 9** A temperature sensor has a transfer function of  $5 \text{ mV}/^\circ\text{C}$  with an accuracy of  $\pm 1\%$ . Find the possible range of the transfer function.

*Solution*

The transfer function range will be  $(\pm 0.01)(5 \text{ mV}/^\circ\text{C}) = \pm 0.05 \text{ mV}/^\circ\text{C}$ . Thus, the range is  $4.95$  to  $5.05 \text{ mV}/^\circ\text{C}$ .

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**EXAMPLE 10** Suppose a reading of  $27.5 \text{ mV}$  results from the sensor used in Example 9. Find the temperature that could provide this reading.

*Solution*

Because the range of transfer function is  $4.95$  to  $5.05 \text{ mV}/^\circ\text{C}$ , the possible temperature values that could be inferred from a reading of  $27.5 \text{ mV}$  are

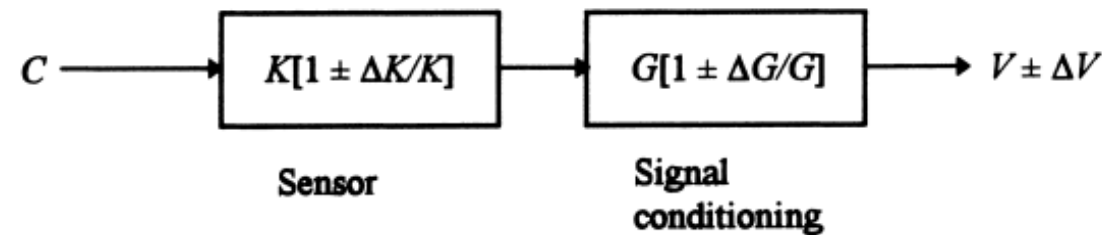
$$(27.5 \text{ mV}) \left( \frac{1}{4.95 \text{ mV}/^\circ\text{C}} \right) = 5.56^\circ\text{C}$$

$$(27.5 \text{ mV}) \left( \frac{1}{5.05 \text{ mV}/^\circ\text{C}} \right) = 5.45^\circ\text{C}$$

Thus, we can be certain only that the temperature is between  $5.45^\circ\text{C}$  and  $5.56^\circ\text{C}$ .

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- Often, one must consider the **overall accuracy** of **many elements** in a process-control loop to represent a process variable.
- Generally, the best way to do this is to express the accuracy of **each element in terms of the transfer functions**.



- The worst-case uncertainty would be the **sum** of the individual uncertainties.
- Statistical analysis teaches us that it is more realistic to use the **root-mean-square (RMS)** representation of system uncertainty.

$$\left[ \frac{\Delta V}{V} \right]_{\text{rms}} = \pm \sqrt{\left( \frac{\Delta K}{K} \right)^2 + \left( \frac{\Delta G}{G} \right)^2}$$

**EXAMPLE 11** Find the system accuracy of a flow process if the transducer transfer function is  $10 \text{ mV}/(\text{m}^3/\text{s}) \pm 1.5\%$  and the signal-conditioning system-transfer function is  $2 \text{ mA}/\text{mV} \pm 0.5\%$ .

## *Solution*

Here we have a direct application of

$$\frac{\Delta V}{V} = \pm \left[ \frac{\Delta K}{K} + \frac{\Delta G}{G} \right]$$

$$\frac{\Delta V}{V} = \pm [0.015 + 0.005]$$

$$\frac{\Delta V}{V} = \pm 0.02 = \pm 2\%$$

so that the net transfer function is  $20 \text{ mA}/(\text{m}^3/\text{s}) \pm 2\%$ . If we use the more statistically appropriate rms approach, the system accuracy would be

$$\begin{aligned} \left[ \frac{\Delta V}{V} \right]_{\text{rms}} &= \pm \sqrt{(0.015)^2 + (0.005)^2} \\ &= \pm 0.0158 \end{aligned}$$

So the accuracy is about  $\pm 1.6\%$ .

- 20** A sensor has a transfer function of  $0.5 \text{ mV}/^{\circ}\text{C}$  and an accuracy of  $\pm 1\%$ . If the temperature is known to be  $60^{\circ}\text{C}$ , what can be said with absolute certainty about the output voltage?

## *Solution*

Well,  $0.5 \text{ mV}/^{\circ}\text{C}$  with a  $\pm 1\%$  accuracy means the transfer function could be  $0.5 \pm 0.005 \text{ mV}/^{\circ}\text{C}$  or  $0.495$  to  $0.505 \text{ mV}/^{\circ}\text{C}$ . If the temperature were  $60^{\circ}\text{C}$  the output would be in the range,  $(0.495 \text{ mV}/^{\circ}\text{C})(60^{\circ}\text{C}) = 29.7 \text{ mV}$  to  $(0.505 \text{ mV}/^{\circ}\text{C})(60^{\circ}\text{C}) = 30.3 \text{ mV}$  or  $30 \pm 0.3 \text{ mV}$ . Which is, of course,  $\pm 1\%$ .

- It is a measure of the change in output of an instrument for a change in input.
- Generally indicated by the **T.F.**
- High sensitivity is desirable in an instrument because a large change in output for a small change in input implies that a measurement may be taken easily.
- Thus, when a temperature transducer outputs 5 mV per degree Celsius, the sensitivity is 5 mv/C

- It is the **minimum measurable** value of the input variable.
- It is expressed in % FS.
- In digital world 1-bit change in binary word
- In some cases, the resolution of a measurement system is **limited** by the **sensitivity** of associated **signal conditioning**.

**EXAMPLE 13** A sensor has a transfer function of 5 mV/°C. Find the required voltage resolution of the signal conditioning if a temperature resolution of 0.2°C is required.

## *Solution*

A temperature change of 0.2°C will result in a voltage change of

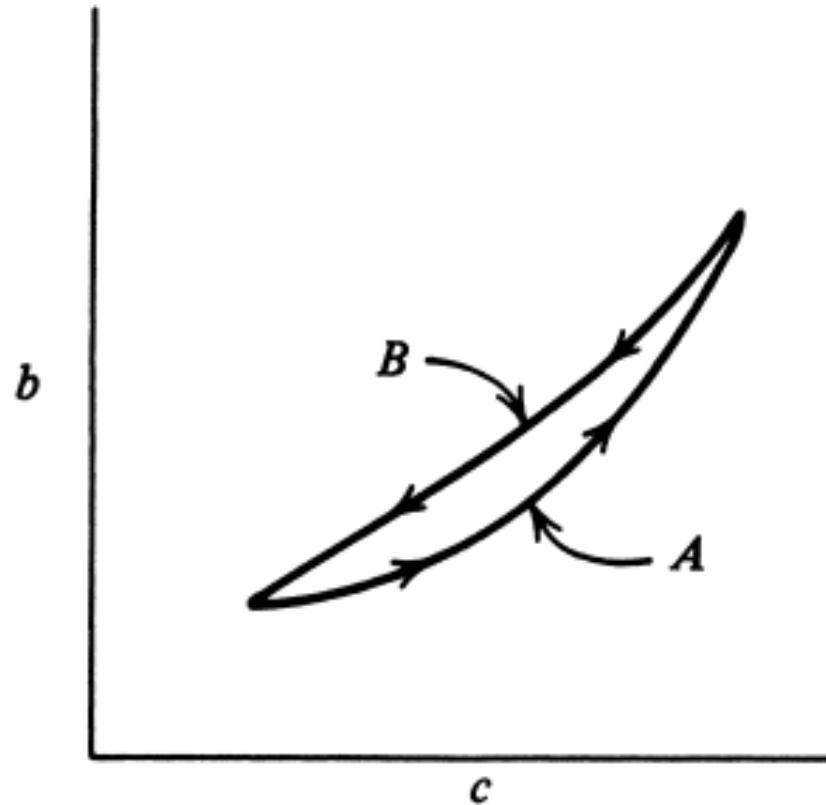
$$\left(5 \frac{\text{mV}}{^{\circ}\text{C}}\right) (0.2^{\circ}\text{C}) = \mathbf{1.0 \text{ mV}}$$

Thus, the voltage system must be able to resolve 1.0 mV.

# Hysteresis:

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- is different reading results for a specific input, depending on whether the input value is approached from higher or lower values.





**END OF LECTURE**

**BEST WISHES**